

CHAPTER EIGHTEEN

MOS Digital Integrated Circuits

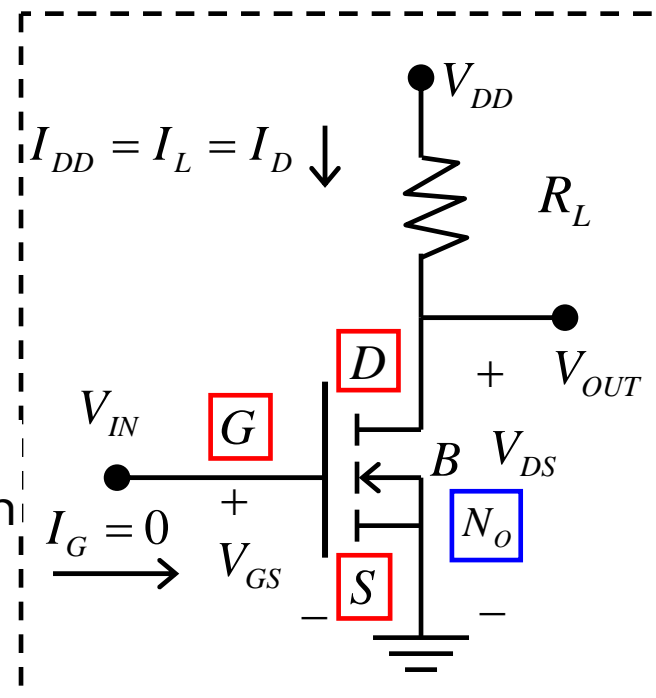
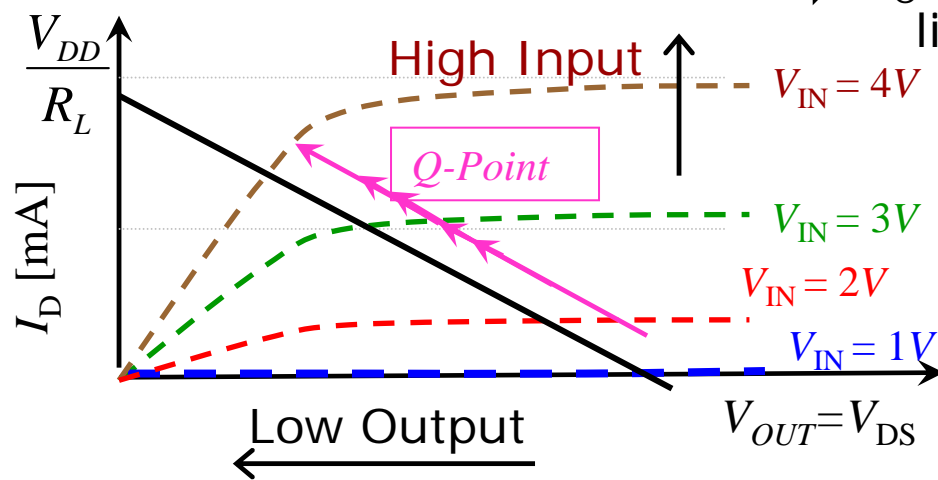
Power Dissipation of Resistor Loaded NMOS Inverter

The currents supplied by V_{DD} for high and low states must be determined

Ch. 18 Output **high** current supplied $I_{DD}(OH)$
For High output, Input is low $\Rightarrow N_O$ is OFF

$$I_{DD}(OH) = 0$$

Output **low** current supplied $I_{DD}(OL)$
For Low output, Input is high $\Rightarrow N_O$ operates in linear region



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$I_{DD}(OL) \rightarrow N_O$ operates in linear region

$$V_{GS} = V_{OH} = V_{DD}$$

$$V_{DS} = V_{OL}$$

$$I_D = \frac{K_n}{2} \left[2 \times (V_{DD} - V_{TN}) V_{DS} - V_{DS}^2 \right] = \frac{V_{DD} - V_{DS}}{R_L}$$

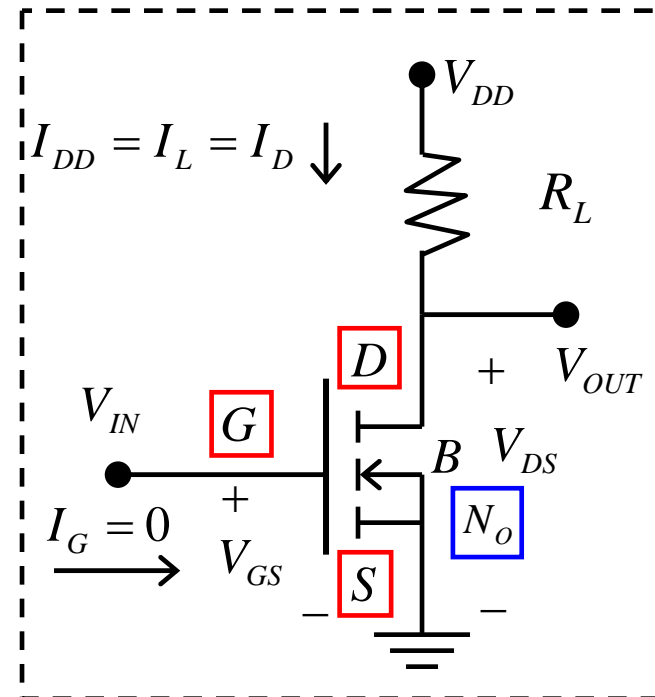
$$V_{DS} = V_{OL} \cong \frac{V_{DD}}{(V_{DD} - V_{TN}) K_n R_L + 1} = \underbrace{V_{DS} \leq (V_{GS} - V_{TN})}_{\text{To ensure that } N_O \text{ operates in linear mode}}$$

To ensure that N_O operates in linear mode

$$I_{DD}(OL) = \frac{K_n}{2} \left[2 \times (V_{DD} - V_{TN}) V_{OL} - V_{OL}^2 \right]$$

Static Power Dissipation $P_{DD}(avg)$

$$P_{DD}(avg) = V_{DD} \left(\frac{I_{DD}(OL) + I_{DD}(OH)}{2} \right) = V_{DD} \left(\frac{I_{DD}(OL)}{2} \right)$$



Power Dissipation of Resistor Loaded NMOS Inverter

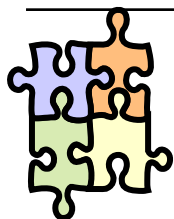
Dynamic Power Dissipation $P_{DD}(\text{dyn})$

$$P_{DD}(\text{dyn}) = C_L \nu (V_{DD})^2$$

C_L is the total load capacitance at the output of the gate

ν is the switching frequency of the gate

Power Dissipation of Resistor Loaded NMOS Inverter



Example

(a) Calculate the static dissipated power in the driver gate for the last example

$V_{DD}=5V$, $V_T=1V$, $k_n=40\mu A/V^2$, $R_L=50k\Omega$,

Solution (Exact Sol.)

Slide 8 of last chapter

$$V_{OL} = \left[V_{DD} - V_{TN} + \frac{1}{K_n R_L} \right] \pm \sqrt{\left[V_{DD} - V_{TN} + \frac{1}{K_n R_L} \right]^2 - \frac{2}{K_n} \frac{V_{DD}}{R_L}}$$

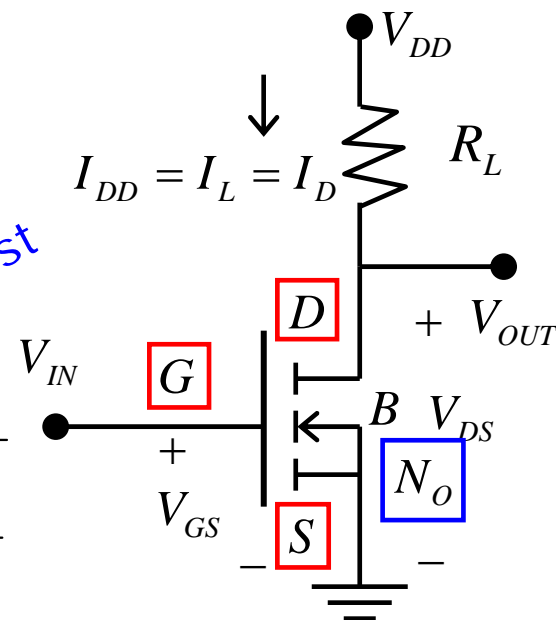
$$V_{OL} = 4.5 \pm 3.905$$

$$V_{OL} = 0.595V \checkmark$$

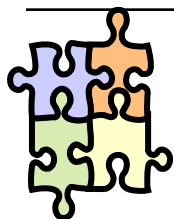
$$V_{OL} = 8.41V \text{ (crossed out)}$$

$$V_{OL} = V_{DS} \leq (V_{GS} - V_{TN}) \quad V_{OL} = V_{DS} \leq (5 - 1)$$

To ensure that N_O operates in linear mode



Power Dissipation of Resistor Loaded NMOS Inverter



Cont.

○ Example

(a) Calculate the static dissipated power in the driver gate for the last example

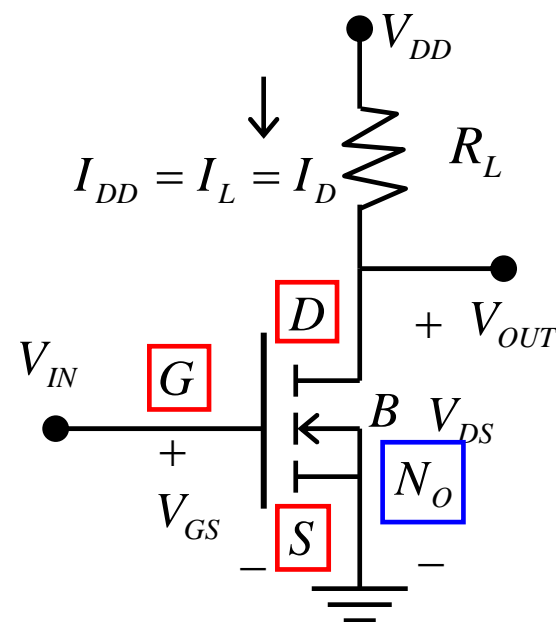
$V_{DD}=5V$, $V_T=1V$, $k_n=40\mu A/V^2$, $R_L=50k\Omega$,

○ Solution (Exact Sol.)

$$V_{OL} = 0.595V$$

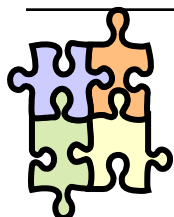
$$I_{DD}(OL) = \frac{V_{DD} - V_{OL}}{R_L} = \frac{5 - 0.595}{50k} = 88.1\mu A$$

$$I_{DD}(OL) = \frac{K_n}{2} \left[2 \times (V_{DD} - V_{TN}) V_{DS} - V_{DS}^2 \right] = 20 \times 10^{-6} (2 \times 4 \times 0.595 - 0.595^2) = 88.1\mu A$$



$$P_{DD}(avg) = 5 \left(\frac{88.1}{2} \right) = 0.22mW$$

Power Dissipation of Resistor Loaded NMOS Inverter



Cont.

○ Example

(a) Calculate the static dissipated power in the driver gate for the last example

$V_{DD}=5V$, $V_T=1V$, $k_n=40\mu A/V^2$, $R_L=50k\Omega$,

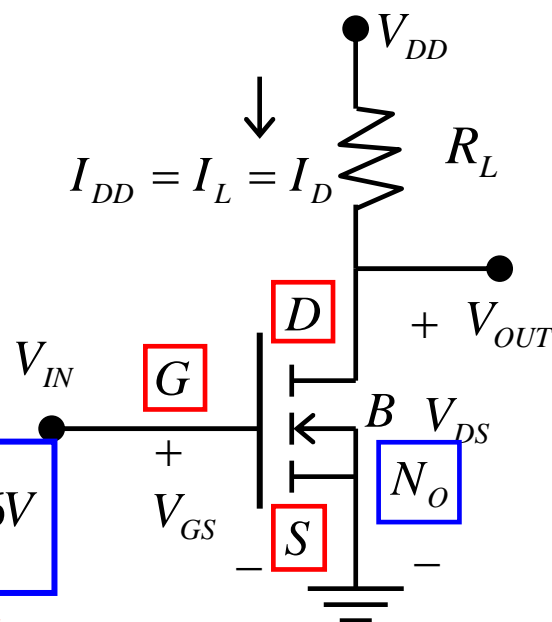
○ Solution (Approx. Sol.)

$$V_{OL} \cong \frac{V_{DD}}{(V_{DD} - V_{TN})K_n R_L + 1} = \frac{5}{(5-1) \times 40 \times 10^{-6} \times 50 \times 10^3} = 0.556V$$

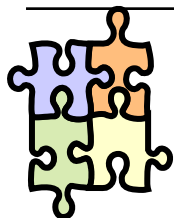
$$I_{DD}(OL) = \frac{V_{DD} - V_{OL}}{R_L} = \frac{5 - 0.556}{50k} = 88.89\mu A$$

$$I_{DD}(OL) = \frac{K_n}{2} [2 \times (V_{DD} - V_{TN})V_{DS} - V_{DS}^2] = 20 \times 10^{-6} (2 \times 4 \times 0.556 - 0.556^2) = 82.8\mu A$$

$$P_{DD}(avg) = 5 \left(\frac{82.8}{2} \right) = 0.207mW$$



Power Dissipation of Resistor Loaded NMOS Inverter



Cont.

○ Example

(b) Calculate the dynamic dissipated power in the driver gate for the last example

$V_{DD}=5V$, $V_T=1V$, $k_n=40\mu A/V^2$, $R_L=50k\Omega$,

$C_L=1pF$, and $\nu=1MHz$

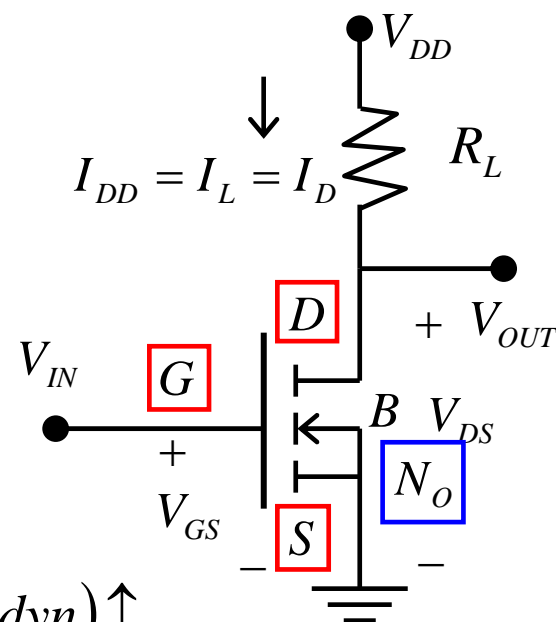
○ Solution

$$P_{DD}(dyn) = C_L \nu (V_{DD})^2$$

$$P_{DD}(dyn) = 10^{-12} \times 10^6 \times 25 = 25\mu W$$

$$C_L \uparrow \Rightarrow P_{DD}(dyn) \uparrow$$

$$C_L = C'_{G1} + C'_{G2} + \dots \text{ parallel}$$



Note: In resistor loaded NMOS inverter, the dynamic dissipated power is less than the static dissipated power

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- HW #10: Solve Problems: 18.1-3,